## CS 61C <br> Spring 2024

## CALL, Boolean Algebra <br> Discussion 5

## 1 Pre-Check

This section is designed as a conceptual check for you to determine if you conceptually understand and have any misconceptions about this topic. Please answer true/false to the following questions, and include an explanation:
1.1 The compiler may output pseudoinstructions.
1.2 The main job of the assembler is to perform optimizations on the assembly code.
1.3 The object files produced by the assembler are only moved, not edited, by the linker.
1.4 The destination of all jump instructions is completely determined after linking.

## 2 Translation

In this question, we will be translating between RISC-V code and binary/hexadecimal values.

Translate the following RISC-V instructions into binary and hexadecimal notations.
1 addi s1 x0 $-24=$
 $\qquad$
2 sh s1 4(t1) $=0 \mathrm{~b}$

In this question, we will be translating between RISC-V code and binary/hexadecimal values.

Translate the following hexadecimal values into the relevant RISC-V instruction.

```
0x234554B7 =
0xFE050CE3 =
```

$\qquad$

## 3 RISC-V Addressing

We have several addressing modes to access memory (immediate not listed):

1. Base displacement addressing adds an immediate to a register value to create a data memory address (used for $\mathrm{lw}, \mathrm{lb}, \mathrm{sw}, \mathrm{sb}$ ).
2. PC-relative addressing uses the PC and adds the immediate value of the instruction (multiplied by 2) to create an instruction address (used by branch and jump instructions).
3. Register Addressing uses the value in a register as an instruction address. For instance, jalr, jr, and ret, where jr and ret are just pseudoinstructions that get converted to jalr

What is the range of 32 -bit instructions that can be reached from the current PC using a branch instruction? Recall that RISC-V supports 16 b instructions via an extension.

What is the maximum range of 32 -bit instructions that can be reached from the current PC using a jump instruction?

Given the following RISC-V code (and instruction addresses), fill in the blank fields for the following instructions (you'll need your RISC-V reference sheet!). Each field refers to a different block of the instruction encoding.

```
0x002cff00: loop: add t1, t2, t0
0x002cff04: jal ra, foo
0x002cff08: bne t1, zero, loop
```





```
0x002cff2c: foo: jr ra ra =
```

$\qquad$

## 4 CALL

The following is a diagram of the CALL stack detailing how C programs are built and executed by machines.


How many passes through the code does the Assembler have to make? Why?

Which step in CALL resolves relative addressing? Absolute addressing?

Describe the six main parts of the object files outputted by the Assembler (Header, Text, Data, Relocation Table, Symbol Table, Debugging Information).

## 5 Boolean Logic

In digital electronics, it is often important to get certain outputs based on your inputs, as laid out by a truth table. Truth tables map directly to Boolean expressions, and Boolean expressions map directly to logic gates. However, in order to minimize the number of logic gates needed to implement a circuit, it is often useful to simplify long Boolean expressions.

We can simplify expressions using the nine key laws of Boolean algebra:

| Name | AND Form | OR form |
| :---: | :---: | :---: |
| Commutative | $\mathrm{AB}=\mathrm{BA}$ | $\mathrm{A}+\mathrm{B}=\mathrm{B}+\mathrm{A}$ |
| Associative | $\mathrm{AB}(\mathrm{C})=\mathrm{A}(\mathrm{BC})$ | $\mathrm{A}+(\mathrm{B}+\mathrm{C})=(\mathrm{A}+\mathrm{B})+\mathrm{C}$ |
| Identity | $1 \mathrm{~A}=\mathrm{A}$ | $0+\mathrm{A}=\mathrm{A}$ |
| Null | $0 \mathrm{~A}=0$ | $1+\mathrm{A}=1$ |
| Absorption | $\mathrm{A}(\mathrm{A}+\mathrm{B})=\mathrm{A}$ | $\mathrm{A}+\mathrm{AB}=\mathrm{A}$ |
| Distributive | $(\mathrm{A}+\mathrm{B})(\mathrm{A}+\mathrm{C})=\mathrm{A}+\mathrm{BC}$ | $\mathrm{A}(\mathrm{B}+\mathrm{C})=\mathrm{AB}+\mathrm{AC}$ |
| Idempotent | $\mathrm{A}(\mathrm{A})=\mathrm{A}$ | $\mathrm{A}+\mathrm{A}=\mathrm{A}$ |
| Inverse | $\mathrm{A}(\overline{\mathrm{A}})=0$ | $\mathrm{~A}+\overline{\mathrm{A}}=1$ |
| De Morgan's | $\overline{\mathrm{AB}}=\overline{\mathrm{A}}+\overline{\mathrm{B}}$ | $\overline{\mathrm{A}+\mathrm{B}}=\overline{\mathrm{A}}(\overline{\mathrm{B}})$ |

Simplify the following Boolean expressions:
(a) $(A+B)(A+\bar{B}) C$
(b) $\bar{A} \bar{B} \bar{C}+\bar{A} B \bar{C}+A B \bar{C}+A \bar{B} \bar{C}+A B C+A \bar{B} C$
(c) $\overline{A(\bar{B} \bar{C}+B C)}$
(d) $\bar{A}(A+B)+(B+A A)(A+\bar{B})$
5.2 Use multiple iterations of De Morgan's laws to prove the identity $\bar{A}+A B=\bar{A}+B$.
5.3 Prove that De Morgan's law can be generalized for the complement of any number of terms.

