1 Pre-Check
This section is designed as a conceptual check for you to determine if you conceptually understand and have any misconceptions about this topic. Please answer true/false to the following questions, and include an explanation:

1.1 Memory sectors are defined by the hardware, and cannot be altered.

1.2 For large recursive functions, you should store your data on the heap over the stack.

1.3 True or False. The goals of floating point are to have a large range of values, a low amount of precision, and real arithmetic results

1.4 True or False. The distance between floating point numbers increases as the absolute value of the numbers increase.

1.5 True or False. Floating Point addition is associative.

2 Memory Management
C does not automatically handle memory for you. In each program, an address space is set aside, separated in 2 dynamically changing regions and 2 'static' regions.

- The Stack: local variables inside of functions, where data is garbage immediately after the function in which it was defined returns. Each function call creates a stack frame with its own arguments and local variables. The stack dynamically changes, growing downwards as multiple functions are called within each other (LIFO structure), and collapsing upwards as functions finish execution and return.

- The Heap: memory manually allocated by the programmer with malloc, calloc, or realloc. Used for data we want to persist beyond function calls, growing upwards to 'meet' the stack. Careful heap management is necessary to avoid Heisenbugs! Memory is freed only when the programmer explicitly frees it!

- Static data: global variables declared outside of functions, does not grow or shrink through function execution.
• Code (or Text): loaded at the start of the program and does not change after, contains executable instructions and any pre-processor macros.

There are a number of functions in C that can be used to dynamically allocate memory on the heap. The following are the ones we use in this class:

• malloc(size_t size) allocates a block of size bytes and returns the start of the block. The time it takes to search for a block is generally not dependent on size.

• calloc(size_t count, size_t size) allocates a block of count * size bytes, sets every value in the block to zero, then returns the start of the block.

• realloc(void *ptr, size_t size) "resizes" a previously-allocated block of memory to size bytes, returning the start of the resized block.

• free(void *ptr) deallocates a block of memory which starts at ptr that was previously allocated by the three previous functions.

For each part, choose one or more of the following memory segments where the data could be located: code, static, heap, stack.

(a) Static variables
(b) Local variables
(c) Global variables
(d) Constants
(e) Machine Instructions
(f) Result of Dynamic Memory Allocation(malloc or calloc)
(g) String Literals

Write the code necessary to allocate memory on the heap in the following scenarios

(a) An array arr of k integers

(b) A string str containing p characters

(c) An n x m matrix mat of integers initialized to zero.

Compare the following two implementations of a function which duplicates a string. Is either one correct? Which one runs faster?

```c
char* strdup1(char* s) {
    int n = strlen(s);
    char* new_str = malloc((n + 1) * sizeof(char));
    for (int i = 0; i < n; i++) new_str[i] = s[i];
    return new_str;
}
```
char* strdup2(char* s) {
    int n = strlen(s);
    char* new_str = calloc(n + 1, sizeof(char));
    for (int i = 0; i < n; i++) new_str[i] = s[i];
    return new_str;
}

What’s the main issue with the code snippet seen here? (Hint: gets() is a function that reads in user input and stores it in the array given in the argument.)

char* foo() {
    char buffer[64];
    gets(buffer);

    char* important_stuff = (char*) malloc(11 * sizeof(char));

    int i;
    for (i = 0; i < 10; i++) important_stuff[i] = buffer[i];
    important_stuff[i] = '\0';
    return important_stuff;
}

3 Linked List

Suppose we’ve defined a linked list struct as follows. Assume *lst points to the first element of the list, or is NULL if the list is empty.

struct ll_node {
    int first;
    struct ll_node* rest;
}

Implement prepend, which adds one new value to the front of the linked list. Hint: why use ll_node** lst instead of ll_node*lst?

void prepend(struct ll_node** lst, int value)
Implement `free_ll`, which frees all the memory consumed by the linked list.

```c
void free_ll(struct ll_node** lst)
```

### 4 Floating Point

The IEEE 754 standard defines a binary representation for floating point values using three fields.

- **The sign** determines the sign of the number (0 for positive, 1 for negative).
- **The exponent** is in **biased notation**. For instance, the bias is -127 which comes from $-(2^{8-1} - 1)$ for single-precision floating point numbers.
- **The significand or mantissa** is akin to unsigned integers, but used to store a fraction instead of an integer.

The below table shows the bit breakdown for the single precision (32-bit) representation. The leftmost bit is the MSB and the rightmost bit is the LSB.

<table>
<thead>
<tr>
<th>1</th>
<th>8</th>
<th>23</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sign</td>
<td>Exponent</td>
<td>Mantissa/Significand/Fraction</td>
</tr>
</tbody>
</table>

For normalized floats:

$$\text{Value} = (-1)^{Sign} \times 2^{\text{Exp} + \text{Bias}} \times 1.\text{Significand}_2$$

For denormalized floats:

$$\text{Value} = (-1)^{Sign} \times 2^{\text{Exp} + \text{Bias} + 1} \times 0.\text{Significand}_2$$

<table>
<thead>
<tr>
<th>Exponent</th>
<th>Significand</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>Anything</td>
<td>Denorm</td>
</tr>
<tr>
<td>1-254</td>
<td>Anything</td>
<td>Normal</td>
</tr>
<tr>
<td>255</td>
<td>0</td>
<td>Infinity</td>
</tr>
<tr>
<td>255</td>
<td>Nonzero</td>
<td>NaN</td>
</tr>
</tbody>
</table>

Note that in the above table, our exponent has values from 0 to 255. When translating between binary and decimal floating point values, we must remember that there is a bias for the exponent.

Convert the following single-precision floating point numbers from binary to decimal or from decimal to binary. You may leave your answer as an expression.

- `0x00000000`
- `8.25`
- `0x00000F00`
- `39.5625`
- `0xFF94BEEF`
- `-\infty`
- `1/3`
5  More Floating Point Representation
As we saw above, not every number can be represented perfectly using floating point. For this question, we will only look at positive numbers.

5.1 What is the next smallest number larger than 2 that can be represented completely?

5.2 What is the next smallest number larger than 4 that can be represented completely?

5.3 What is the largest odd number that we can represent? Hint: Try applying the step size technique covered in lecture.