CS61C Fall 2025

C, Floating Point Discussion 3

1 Floating Point

1.1 Convert the following single-precision floating point numbers from hexadecimal to decimal or from decimal to hexadecimal using the IEEE 754 Floating Point Standard. You may leave your answer as an expression.

a) 8.25

Answer: 0x41040000

First, we write 8.25 into binary. Splitting 8.25 into its integer and decimal portions, we can determine that 8 will be encoded in binary as 1000 and 0.25 will be .01 (the 1 corresponds to the 2^{-2} place). So, 8.25 = 1000.01. In normalized form, we get $1.00001_2 \times 2^3$.

b) 39.5625

Answer: 0x421E4000

c) 0x00000F00

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Answer:
$$(2^{-12} + 2^{-13} + 2^{-14} + 2^{-15}) * 2^{-126}$$

For 0x00000F00, splitting up the hexadecimal gives us a sign bit and exponent bit of 0, and a significand of 0b 000 0000 0000 1111 0000 0000. Since the exponents bits are 0, we know that this is a denormalized positive number. We can find out the true power by adding the bias + 1 to get a power of -126.

Then, we can evaluate the mantissa by inspecting the bits that are 1 to the right of the decimal point, and finding the corresponding negative power of two. This results in the mantissa evaluated as $2^{-12} + 2^{-13} + 2^{-14} + 2^{-15}$. Combining these get the extremely small number $(-1)^0 * 2^{-126} * (2^{-12} + 2^{-13} + 2^{-14} + 2^{-15})$

d) 0

Answer: 0x00000000

To represent zero in floating point, the significand will be zero but we need to set the correct exponent. Recall that any non-zero exponent will indicate a *normalized* float which means the significand has a leading 1. Zero's binary representation does not have a leading 1, so we need an exponent of zero to indicate a *denormalized* float which implies a leading zero in front of the significand. Fortunately, this nicely works out to represent zero as $0 \times 0 \times 0 \times 0 \times 0 = 0$.

e) 0xFF94BEEF

Answer: NaN

Certain exponent fields are reserved for representing special values. Floating point representations with exponents of 255 and a zero significand are reserved for $\pm \infty$, and exponents of 255 with a nonzero significand are reserved for representations of NaN. Deconstructing the fields of this number gives an exponent of 0b111111111 = 255 and a nonzero significand which indicates that this represents NaN. Note that there are many possible ways to represent NaN.

f) ∞

Answer: 0x7F800000

g) 1/3

Answer: N/A - impossible to represent in single-precision floating point, we can only approximate it

2 More Floating Point

As we saw above, not every number can be represented perfectly using floating point. For this question, we will only look at positive numbers.

2.1 What is the next smallest number larger than 2 that can be represented completely?

Answer: $2 + 2^{-22}$

First,we start at the number 2 and write it in the normalized form. Then we increment the number by the smallest amount possible, which is the same as incrementing the significand by 1 at the rightmost location, which adds 2^{-22} .

Normalized: $2=10.000...=1.000...00\times 2^1$ Increment: $2=(1.000...00+2^{-23})\times 2^1=(1+2^{-23})\times 2=2+2^{-22}$

2.2 What is the next smallest number larger than 4 that can be represented completely?

Answer: $4 + 2^{-21}$

Similarly, we write 4 in its normalized form, and increment it by the smallest amount possible. This is the same as incrementing the significand by 1 at the rightmost location.

Normalized: $4=100.000...=1.000...00\times 2^2$ Increment: $(1.000...00+2^{-23})\times 2^2=(1+2^{-23})\times 4=4+2^{-21}$

2.3 What is the largest odd number that we can represent? Hint: at what power can we only represent even numbers?

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Answer: $2^{24} - 1$

To find the largest odd number we can represent, we want to find when odd numbers will stop appearing. Because we are always multiplying the significand by a power of 2^x , we will only be able to represent even numbers when the exponent grows large enough. In particular, odd numbers will stop appearing when the significand's LSB has a step size (distance between each successive number) of 2, so the largest odd number will be the first number with a step size of 2, subtracted by 1. After this number, only even numbers can be represented in floating point.

We can think of each binary digit in the significant as corresponding to a different power of 2 to get to a final sum. For example, 0b1011 can be evaluated as $2^3 + 2^1 + 2^0$, where the MSB is the 3rd bit and corresponds to 2^3 and the LSB is the 0th bit at 2^0 .

We want our LSB to correspond to 2^1 , so by counting the number of mantissa bits (23) and including the implicit 1, we get a total exponent of 24. The smallest number with this power would have a mantissa of 00..00, so after taking account of the implicit 1 and subtracting, this gives $2^{24} - 1$

3 C Generics

3.1 **True** or **False**: In C, it is possible to directly dereference a **void** * pointer, e.g.

```
... = *ptr;
```

False. To dereference a pointer, we must know the number of bytes to access from memory at compile time. A void * pointer contains the address for an arbitrary region of memory without a known size, so they cannot be dereferenced – they must be typecast beforehand (e.g. ... = *((int *) ptr))

3.2 Generic functions (i.e., generics) in C use **void** * pointers to operate on memory without the restriction of types. Generic pointers do not support dereferencing, as the number of bytes to access from memory is not known at compile-time. They instead use byte handling functions such as memcpy and memmove.

Implement rotate, which will prompt the following program to generate the provided output.

```
int main(int argc, char *argv[]) {
  int array[10] = {1, 2, 3, 4, 5, 6, 7, 8, 9, 10};
  print_int_array(array, 10);
  rotate(array, array + 5, array + 10);
  print_int_array(array, 10);
  rotate(array, array + 1, array + 10);
  print_int_array(array, 10);
  rotate(array + 4, array + 5, array + 6);
  print_int_array(array, 10);
  return 0;
}
```

Output:

```
$ ./rotate
Array: [1, 2, 3, 4, 5, 6, 7, 8, 9, 10]
Array: [6, 7, 8, 9, 10, 1, 2, 3, 4, 5]
Array: [7, 8, 9, 10, 1, 2, 3, 4, 5, 6]
Array: [7, 8, 9, 10, 2, 1, 3, 4, 5, 6]
```

```
void rotate(void *front, void *separator, void *end) {
  size_t width = (char *) end - (char *) front;
  size_t prefix_width = (char *) separator - (char *) front;
  size_t suffix_width = width - prefix_width;
  char temp[prefix_width];
  memcpy(temp, front, prefix_width);
  memmove(front, separator, suffix_width);
  memcpy((char *) end - prefix_width, temp, prefix_width);
}
```

See slides provided under "Discussion Resources" for a visual walkthrough of the solution.