

Solutions last updated: Wednesday, November 5, 2025

PRINT Your Name: _____

PRINT Your Student ID: _____

PRINT the Name and Student ID of the person to your left: _____

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You have 170 minutes. There are 7 questions of varying credit. (100 points total)

Question:	1	2	3	4	5	6	7	Total
Points:	22	12	15	23	15	13	0	100

For questions with **circular bubbles**, you may select only one choice.

- ☐ Unselected option (Completely unfilled)
- ☒ Don't do this (it will be graded as incorrect)
- ☒ Only one selected option (completely filled)

For questions with **square checkboxes**, you may select one or more choices.

- ☒ You can select
- ☒ multiple squares
- ☒ (Don't do this)

Anything you write outside the answer boxes or you ~~cross-out~~ will not be graded. If you write multiple answers, your answer is ambiguous, or the bubble/checkbox is not entirely filled in, we will grade the worst interpretation. For coding questions with blanks, you may write at most one statement per blank and you may not use more blanks than provided.

If an answer requires hex input, you must only use capitalized letters (0xBOBACAFE instead of 0xb0bacafe). For hex and binary, please include prefixes in your answers unless otherwise specified, and do not truncate any leading 0's. For all other bases, do not add any prefixes or suffixes.

As a member of the UC Berkeley community, I act with honesty, integrity, and respect for others. I will follow the rules of this exam.
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Acknowledge that you have read and agree to the honor code above and sign your name below:

Clarifications made during the exam:

Q6: The circuit component delays are as follows:

- T_{not} : 1 ps
- T_{and} : 2 ps
- T_{or} : 3 ps
- $T_{\text{clk_to_q}}$: 4 ps
- T_{setup} : 10 ps

Q3.4: RISC-V 16I only applies to the question subpart asking for the range of target addresses for branch instructions. `diff_sign` and the rest of the question uses 32-bit RISC-V.

Q1 Trees...

(22 points)

Suppose that we implement a binary tree using the `node_t` struct, defined as follows:

```
1 typedef struct Node {
2     char name[6];
3     struct Node *left, *right;
4     int64_t *data;
5 } node_t;
```

For Q1.1 – Q1.14, you may assume that:

- We are on a **64-bit** system.
- `sizeof(size_t) == sizeof(void*) == 8`
- All pointers are word-aligned
- In any `node_t`, `name` is a valid string containing at most 5 characters.

Q1.1 (2 points) What is `sizeof(node_t)`?

32 bytes

(10 points) Implement the `node_new` function. This function should create a new `node_t` on the heap with the provided argument as its `name`, and return a pointer to the newly created `node_t` struct.

node_new: Initializes a node_t with the given name.		
Arguments	char *name	The name of the <code>node_t</code> to be created. Assume <code>name</code> points to a valid string and <code>strlen(name) <= 5</code> .
	int64_t data	The value to be stored in the newly created <code>node_t</code>
Return value	node_t *	A pointer to the newly created <code>node_t</code> struct.

```
1 node_t* node_new(char *name, int64_t data) {
2     node_t *n = calloc(1, sizeof(node_t));
3     if (!n) return NULL;
4     memcpy(n->name, name, strlen(name) + 1);
5     n->data = malloc(sizeof(int64_t));
6     if (!(n->data)) return NULL;
7     *(n->data) = data;
8     return n;
9 }
```

Useful C function prototypes:

```
size_t strlen(const char *s);
void *memcpy(void *dest, const void *src, size_t n);
```

(4 points) Implement the **free_tree** function. This function should free all memory allocated for the given binary tree rooted at **t**, including all **data** and subtrees. You may assume that all nodes in the tree are heap-allocated.

```
1 void free_tree(node_t *t) {  
2     if (!t) return;  
3     free_tree(t->left);           Q1.9  
4     free_tree(t->right);        Q1.10  
5     free(t->data);              Q1.11  
6     free(t);                   Q1.12  
7 }
```

Solution: The first three lines free any child nodes that may exist, alongside the heap-allocated data. These lines are interchangeable. Note that the name of the node does not have to be freed because the name is stored as part of the **Node** struct itself rather than being separately stored on the heap.

After the first three lines, we can then free the current node, **t** to end this function. Freeing **t** any earlier would cause the struct members (like **left** and **data**) to become inaccessible.

For Q1.13 – Q1.14, assume that you have finished running the **node_new** function but have not returned from the function yet. For each of the following symbols, indicate which segment of memory it is stored in.

Q1.13 (1 point) **memcpy**

☐ Stack ☐ Heap ☐ Static ☒ Code

Q1.14 (1 point) **n->name**

☐ Stack ☒ Heap ☐ Static ☐ Code

Q1.15 The Call 🛡️👉

For each of the following questions, select the step of CALL that performs the operation.

Q1.15.1 (1 point) Copies the executable file into memory to prepare for execution.

☐ Compiler ☐ Assembler ☐ Linker ☒ Loader

Q1.15.2 (1 point) Replaces the immediate in **la label** with its final value. (**label** is defined in a different file than the **la** instruction)

☐ Compiler ☐ Assembler ☒ Linker ☐ Loader

(Question 1 continued...)

Q1.15.3 (1 point) Expands pseudoinstructions into their corresponding machine instructions.

☐ Compiler ☒ Assembler ☐ Linker ☐ Loader

Q1.15.4 (1 point) Takes high-level language code as input.

☒ Compiler ☐ Assembler ☐ Linker ☐ Loader

Q2 It Takes Two 🧑🧑

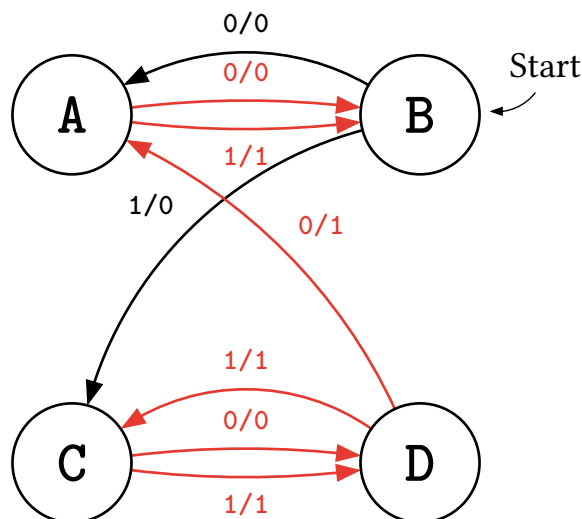
(12 points)

Complete the below FSM that swaps the left and right bit in each pair of bits. For example, if we let each letter represent a bit, the input **stuvwxyz-** should yield an output of **0tsvuxwzy**, as shown in the table below.

Example Input	stuvwxyz-
Example Output	0t sv uxwzy

Assume the first output is always a 0 (since you can't output bit **t** until you see it), and the - at the end represents some input bit so that **y** can be outputted.

Q2.1 (12 points) Fill in the table describing the state transitions of this FSM. Two transitions have been given to you in the diagram and filled out in the table for your reference.



Current State	Input	Next State				Output	
A	0	☐ A	☒ B	☐ C	☐ D	☒ 0	☐ 1
A	1	☐ A	☒ B	☐ C	☐ D	☐ 0	☒ 1
B	0	☒ A	☐ B	☐ C	☐ D	☒ 0	☐ 1
B	1	☐ A	☐ B	☒ C	☐ D	☒ 0	☐ 1
C	0	☐ A	☐ B	☐ C	☒ D	☒ 0	☐ 1
C	1	☐ A	☐ B	☐ C	☒ D	☐ 0	☒ 1
D	0	☒ A	☐ B	☐ C	☐ D	☐ 0	☒ 1
D	1	☐ A	☒ B	☐ C	☐ D	☐ 0	☒ 1

Solution: This FSM is really tricky! It's a little easier to understand what the FSM is doing by breaking down the role of each state.

A

- The previous input was the first bit of the current pair and was 0
- The next input is the second bit of the pair, and should be output immediately

C

- The previous input was the first bit of the current pair and was 1
- The next input is the second bit of the pair, and should be output immediately

B

- The first bit of the previous pair was 0 and should be output at the next transition
- The next input is the first bit of a new pair

D

- The first bit of the previous pair was 1 and should be output at the next transition
- The next input is the first bit of a new pair

Notice in the example given that the 2nd bit of each pair is output immediately, but the 1st bit of each pair is 'delayed' by two FSM transitions. This is why all states in our FSM help store information about the 1st bit, allowing us to stall time before outputting it.

As an example of how this FSM might function, consider the input 10010.

- B to C / Input: 1 / Output: 0
 - The first bit of this set is 1, so we move to C to help store this information.
 - Since the previous state was B, the output will be 0
- C to D / Input: 0 / Output: 0
 - C always transitions to D to continue storing information about the first bit, which was 1
 - The second bit of the pair, 0, is output immediately
- D to A / Input: 0 / Output: 1
 - The first bit of the next pair is 0, so we move to A to help store this information
 - During this transition, we finally output the first bit of the previous pair, which was 1, since we're transitioning from state D
- A to B / Input: 1 / Output: 1
 - A always transitions to B to continue storing information about the first bit, which was 0
 - The second bit of the pair, 1, is output immediately
- B to A / Input: 0 / Output: 0
 - The first bit of the previous pair, which was 0, is now output since we're transitioning from state B
 - If this input kept going, 0 would be the first bit of the next pair and there would be a transition to A to store this information

Q3 Jump Up, Super Star! ★

(15 points)

Q3.1 (3 points) Translate the instruction on line 3 to hexadecimal RISC-V machine code.

```
1 label: addi a1 x0 1
2         slli a1 a1 2
3         bne a3 t2 label
```

0xFE769CE3

Q3.2 (1 point) The `imm[0]` bit of a branch instruction can be either 0 or 1.

☐ True ☒ False

Q3.3 (2 points) If a branch instruction is taken, what is the maximum number of **32-bit** instructions we can jump backwards by? You may express your answer as a power of 2.

2^{10}

Q3.4 (4 points) Consider an ISA called RISC-V 16I, where **every instruction is 16 bits long**.

RISC-V 16I uses a 6-bit, 2's complement signed immediate for B-type instructions, with an implied 0 as the LSB. Everything else about B-type instructions remains the same. What is the range of target addresses for branch instructions, **inclusive**? Write your answers in terms of powers of 2.

$\left[PC - 2^6, PC + 2^6 - 2 \right]$

(5 points) Implement the `diff_sign` function. You **may only** use the `a0` and `a1` registers in your solution.

`diff_sign`: Determines whether registers `a0` and `a1` have different signs.

Arguments	a0	a nonzero 2's complement integer
	a1	a nonzero 2's complement integer
Return value	a0	0 if the inputs are both positive or both negative, 1 if they have different signs

```
1 diff_sign:
2     xor a0 a0 a1
3         srli a0 a0 31
4         jr ra
```

Q4 The World Revolving ♠

(23 points)

Binary search is an algorithm to find the index of some desired value in a sorted array `arr`. The below C implementation of binary search is given for your reference. For this question, you may assume that `target` appears in `arr`.

```
1 int binary_search(int* arr, int left, int right, int target) {
2     int mid = (left + right) / 2; // C division rounds down
3     if arr[mid] == target {
4         return mid;
5     } else if target < arr[mid] {
6         return binary_search(arr, left, mid - 1, target);
7     } else {
8         return binary_search(arr, mid + 1, right, target);
9     }
10 }
```

(20 points) Implement the `binary_search` function.

binary_search: determines the index of the value in a3 in the array a0.		
Arguments	a0	A pointer to a sorted array with integers
	a1	Left index; initially set as zero
	a2	Right index; initially set as length of array - 1
	a3	The target value we want to find
Return value	a0	The index of the target element

(Question 4 continued...)

```
1  binary_search:
2      # prologue omitted
3      add s0 a1 a2
4
5      srli s0 s0 1
6      slli s1 s0 2
7      add s1 a0 s1
8      lw s2 0(s1)
9      beq a3 s2 found
10     blt a3 s2 search_left
11
12     found:
13         mv a0 s0
14         j done
15     search_left:
16
17     addi a2 s0 -1
18     jal ra binary_search
19     j done
20
21     search_right:
22
23     addi a1 s0 1
24     jal ra binary_search
25
26     done:
27     # epilogue omitted
28     jr ra
```

Q4.11 (3 points) Select which registers need to be saved in the prologue and restored in the epilogue for `binary_search` to satisfy calling conventions.

☐ a0 ☒ s0 ☐ a1 ☒ s1 ☐ a2 ☒ s2 ☒ ra ☐ None of the above

Grading: If you used a temporary register or s1 in Q4.3, s2 does not have to be saved/restored.

Q5 On Little Cat Feet ☀

(15 points)

We want to implement a new RISC-V instruction **smaller rd rs1 rs2** that does the following:

```

1 if (R[rs1] < R[rs2])
2   R[rd] = R[rs1]
3 else
4   R[rd] = R[rs2]
```

Q5.1 (2 points) What instruction type would be the most suitable for **smaller**?

- ☒ R ☐ I* ☐ B ☐ J
☐ I ☐ S ☐ U ☐ No existing instruction type works

Solution: When considering an instruction type to use for a new instruction, it's most important to consider the arguments required by the instruction. In this case, the new **smaller** instruction requires three register arguments, which an R-type instruction type is well-suited to handle.

Q5.2 (1 point each) We decide to modify **only** the ALU to implement this (and select a new **ALUSel** value to trigger any potential new operations). What are the values of the control signals necessary to implement **smaller**? Fill in * if the value of the control signal does not matter.

PCSel	☒ PC + 4	☐ ALU	☐ Depends on BrEQ and BrLT	☐ *
ASel	☒ Reg	☐ PC	☐ Depends on BrEQ and BrLT	☐ *
BSEL	☒ Reg	☐ Imm	☐ Depends on BrEQ and BrLT	☐ *
MemRW	☒ Read	☐ Write	☐ Depends on BrEQ and BrLT	☐ *
RegWEn	☒ 1	☐ 0	☐ Depends on BrEQ and BrLT	☐ *
ImmSel	☐ I ☐ B ☐ S	☐ Depends on BrEQ and BrLT	☒ *	
WBSEL	☒ ALU ☐ Mem ☐ PC + 4	☐ Depends on BrEQ and BrLT	☐ *	

(Question 5 continued...)

Suppose we keep the ALU modification but make the **smaller** instruction do the following instead:

```
1 if (R[rs1] < R[rs2])
2   R[rd] = R[rs1]
3 else
4   Mem[R[rd]] = R[rs2] # New change
```

Q5.3 (2 points) What instruction type would be the most suitable for the new version of **smaller**?

- ☒ R ☐ I* ☐ B ☐ J
☐ I ☐ S ☐ U ☐ No existing instruction type works

Solution: Despite the added functionality in this new version of **smaller**, the arguments of this instruction do not change and we can still use an R-type structure to represent them.

Q5.4 (4 points) What additional changes, if any, would we need to make to our single-cycle datapath for us to implement this (with as few changes as possible)? Select all that apply.

- ☐ Add a new read input to the RegFile for a third register value.
☒ Add a new read output to the RegFile for a third read register value
☐ Add a new WriteData and WriteIndex input to the RegFile
☐ Add a third possible value for **ASel** and update the corresponding MUX/control logic
☐ Add a third possible value for **BSe1** and update the corresponding MUX/control logic
☐ Add a third possible value for **PCSe1** and update the corresponding MUX/control logic
☐ Add a new read input to DMEM for a second memory read output.
☒ Add a MUX in front of DMEM's **addr** input and a new control line to control it
☐ Add a MUX in front of DMEM's **wdata** input and add a new control line to control it
☐ Add a fourth possible value for **WBSe1** and update the corresponding MUX/control logic
☐ None of the above

Q6 StarDrop Saloon 🍹

(13 points)

Q6.1 (3 points) Write a Boolean expression for the below table in terms of A, B, and C. For full credit, you may use at most 2 operators. Your answer may consist of the following operators and symbols:

Operators			Symbols		
NOT	AND	OR	Inputs	Constants	Parentheses
!A	A * B	A + B	A, B, C	0, 1	()

A	B	C	Output
0	0	0	1
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	0
1	1	1	1

Output = !B + C

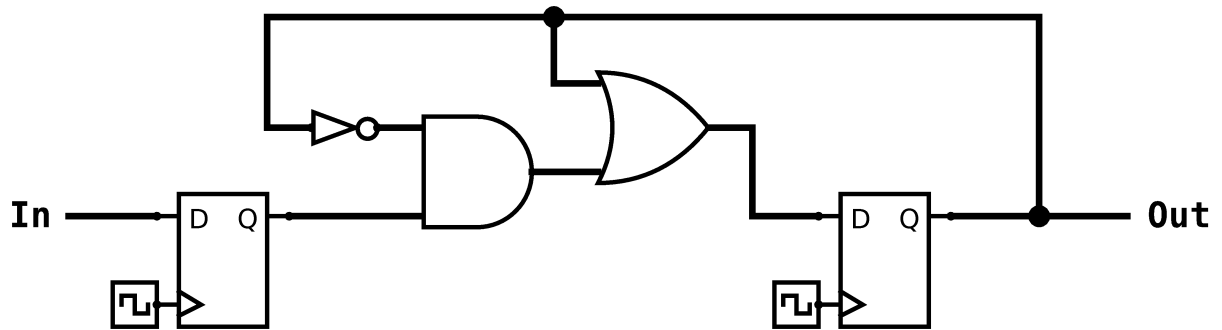
Solution: Observe that the third and second-to-last rows are the only rows with an output of 0. We can express that using the following boolean expression:

$$\begin{aligned}
 \overline{ABC} + ABC &= (\overline{A} + A)\overline{BC} \\
 &= \overline{BC} \\
 &= \overline{B} + C
 \end{aligned}$$

The rest of this page left intentionally (mostly) blank.

(Question 6 continued...)

For Q6.2 – Q6.4, consider the following circuit and timings



with the following circuit times for the components used above

$$t_{\text{setup}} = 10 \text{ ps} \quad t_{\text{clk-to-q}} = 4 \text{ ps} \quad t_{\text{NOT}} = 1 \text{ ps} \quad t_{\text{AND}} = 2 \text{ ps} \quad t_{\text{OR}} = 3 \text{ ps}$$

Q6.2 (3 points) What is the minimum clock period this circuit can have to consistently exhibit well-defined behavior?

20ps

Solution: For this solution, we are starting from the output of the second register, going through the NOT, AND, and OR gates and ending at the input of the same register.

$$\begin{aligned} t_{\text{clk-period}} &\geq t_{\text{clk-to-q}} + t_{\text{longest-combinational-delay}} + t_{\text{setup}} \\ &= t_{\text{clk-to-q}} + t_{\text{NOT}} + t_{\text{AND}} + t_{\text{OR}} + t_{\text{setup}} \\ &= 4 + 1 + 2 + 3 + 10 \\ &= 20\text{ps} \end{aligned}$$

Q6.3 (3 points) What is the range of possible hold time values (in ps) for this circuit to consistently exhibit well-defined behavior?

E.g. if the hold time had to be bigger than 99ps you would write $99\text{ps} \leq t_{\text{hold}}$ and leave the second box blank. If the hold time had to be between 57ps and 88ps, you would write $57\text{ps} \leq t_{\text{hold}} \leq 88\text{ps}$

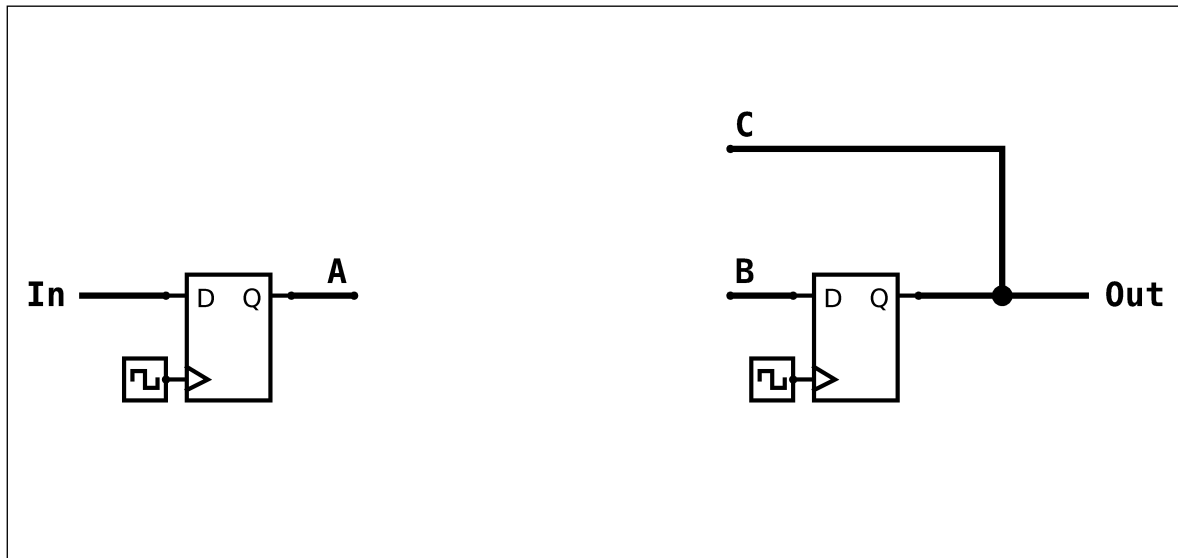
0ps	$\leq t_{\text{hold}} \leq$	7ps
-----	-----------------------------	-----

Solution: The shortest combinational path in this circuit involves just a single OR gate and starts at the output of the second register, goes through the OR gate, and ends at the input of the same register. Using the formula for hold time, we have

$$\begin{aligned} 0 \leq t_{\text{hold}} &\leq t_{\text{clk-to-q}} + t_{\text{shortest-combinational-delay}} \\ &= t_{\text{clk-to-q}} + t_{\text{OR}} \\ &= 4 + 3 \\ &= 7\text{ps} \end{aligned}$$

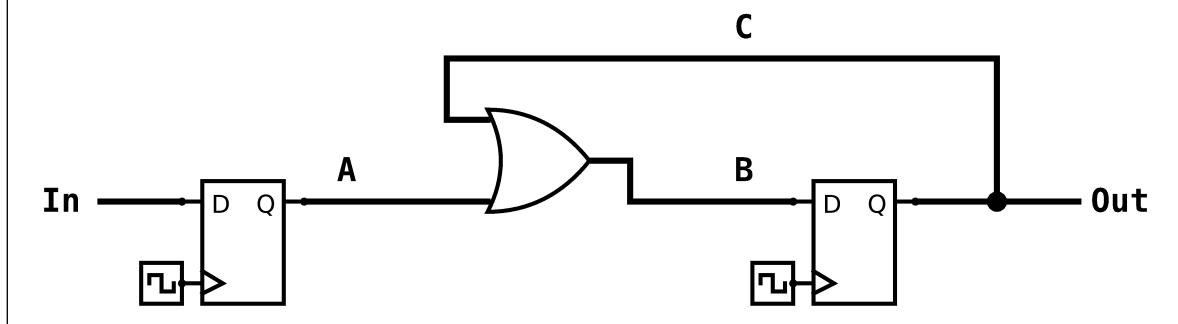
(Question 6 continued...)

Q6.4 (4 points) To increase the maximum clock frequency, simplify and reconnect the circuit by appropriately joining the wires labeled (A, B, C) and drawing **at most one** gate, ensuring that the circuit's functionality remains identical to the original.



Solution: Add an OR gate that takes A and C as inputs to produce B as the output. We can express the circuit in Boolean algebra and simplify it as follows:

$$\begin{aligned} B &= A * \overline{C} + C \\ &= (A + C) * (\overline{C} + C) \quad \text{by the distributive property} \\ &= A + C \end{aligned}$$



Q7 *The Finishing Touch* 🥤👤

(0 points)

These questions will not be assigned credit. Feel free to leave them blank.

Q7.1 What is the common theme across these question names? What references do you recognize? :->

Solution: All the question names (and emoji) are based on video game soundtracks!

Trees - OMORI

The Call - League of Legends

It Takes Two - It Takes Two

Jump Up, Super Star! - Super Mario Odyssey

The World Revolving - DELTARUNE

On Little Cat Feet - Oneshot

StarDrop Saloon - Stardew Valley

The Finishing Touch - Cuphead: The Delicious Last Course

(Question 7 continued...)

Q7.2 If there's anything else you want us to know, or you feel like there was an ambiguity in the exam, please put it in the box below.

For ambiguities, you must qualify your answer and provide an answer for both interpretations. For example, "if the question is asking about A, then my answer is X, but if the question is asking about B, then my answer is Y". You will only receive credit if it is a genuine ambiguity and both of your answers are correct. We will only look at ambiguities if you request a regrade.

Solution: If you're reading this, you get a cookie! 🍪