# CS61C Spring 2025

Boolean Algebra, CALL Discussion 7

### 1 Boolean Logic

**1.1** Simplify the following Boolean expressions:

(a)  $(A+B)(A+\overline{B})C$ 

(b)  $\overline{A} \,\overline{B} \,\overline{C} + \overline{A} \,B \,\overline{C} + A \,B \,\overline{C} + A \,\overline{B} \,\overline{C} + A \,B \,C + A \,\overline{B} \,C$ 

(c)  $\overline{A(\overline{B}\,\overline{C} + BC)}$ 

(d)  $\overline{A}(A+B) + (B+AA) \left(A+\overline{B}\right)$ 

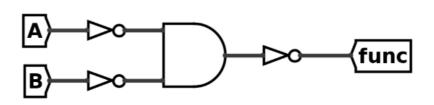
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## 2 Digital Logic Simplification

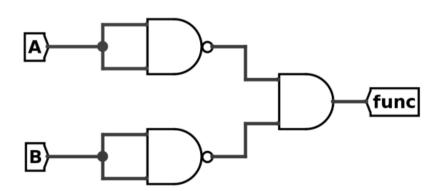
For the following digital logic circuits:

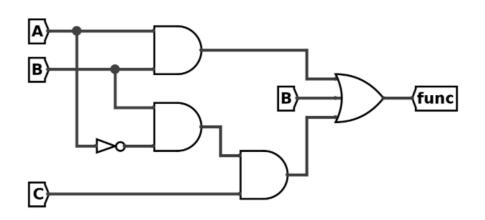
- 1. Write a boolean algebra expression that corresponds the physical circuit.
- 2. Simplify the expression and draw the simplified circuit.

2.1



2.2





2.3

2.4 Why might it be useful to simplify logic circuits?

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### 3 Combinational Logic from Truth Tables

For this question, we have a single 3-bit input and a single 4-bit output. We want to design a combinational logic circuit to achieve the desired output given the appropriate combinations of input bits (Input=001  $\implies$  Output=0011, and so on...). Here is the truth table we wish to implement:

Input	Out
000	0001
001	0011
010	1111
011-111	xxxx

The x's for the final entry of the table indicate that any output is valid for the case that Input is 011, 100, 101, 110, and 111

3.1 Write out and simplify boolean expressions for each of the output bits Out[3], Out[2], Out[1], and Out[0] in terms of the input bits In[2], In[1], In[0].

3.2 Draw out the boolean circuit based on your simplified expressions above. You may use constants 0 and 1, and the logic gates AND, OR, NOT.

### 4 Two-Pass Assembly

Consider the following assembly code. Assume that **printf** exists in the C standard library and that **msg** exists at an unknown address in the .data section.

```
Address | Assembly
-----|------
.data
       | msg: .string "Hello World"
       .text
       0x0C
       add t0, x0, x0
0x10
       addi t1, x0, 4
0x14
                beq t0, t1, end
       | loop:
0x18
       addi a0, a0, 1
                     aO, msg
0x1C
       la
                                 // load address of `msg`
0X20
                jal ra, printf
       0X24
       | n:
                addi t0, t0, 1
0X28
       loop
                j
OX2C
       | end:
                ret
```

4.1 This code is output from the \_\_\_\_\_ (Compiler, Assembler, Linker, or Loader) and \_\_\_\_\_ (may / may not) contain pseudoinstructions.

4.2 Assume we are using a two-pass assembler. Fill out the symbol table after the first pass (top-to-bottom) of the assembler. Not all lines may be used.

Symbol Table	
Label	Address

4.3 After the first pass of the assembler, which of the instructions do not have their addresses fully resolved?

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4.4 After the second pass of the assembler but before the linker, which of the instructions do not have their addresses fully resolved?