# CS61C Summer 2025

# 1 Floating Point

1.1 Convert the following single-precision floating point numbers from hexadecimal to decimal or from decimal to hexadecimal using the IEEE 754 Floating Point Standard. You may leave your answer as an expression.

#### a) 8.25

#### Answer: 0x41040000

First, we write 8.25 into binary. Splitting 8.25 into its integer and decimal portions, we can determine that 8 will be encoded in binary as 1000 and 0.25 will be .01 (the 1 corresponds to the  $2^{-2}$  place). So, 8.25 = 1000.01. In normalized form, we get  $1.00001_2 \times 2^3$ .

#### b) 39.5625

#### Answer: 0x421E4000

#### c) 0x0000F00

#### 2 Floating Point, RISC-V

Answer:  $(2^{-12} + 2^{-13} + 2^{-14} + 2^{-15}) * 2^{-126}$ 

For 0x00000F00, splitting up the hexadecimal gives us a sign bit and exponent bit of 0, and a significand of 0b 000 0000 0000 1111 0000 0000. Since the exponents bits are 0, we know that this is a denormalized positive number. We can find out the true power by adding the bias + 1 to get a power of -126.

Then, we can evaluate the mantissa by inspecting the bits that are 1 to the right of the decimal point, and finding the corresponding negative power of two. This results in the mantissa evaluated as  $2^{-12} + 2^{-13} + 2^{-14} + 2^{-15}$ . Combining these get the extremely small number  $(-1)^0 * 2^{-126} * (2^{-12} + 2^{-13} + 2^{-14} + 2^{-15})$ 

### d) 0

### Answer: 0x0000000

To represent zero in floating point, the significand will be zero but we need to set the correct exponent. Recall that any non-zero exponent will indicate a *normalized* float which means the significand has a leading 1. Zero's binary representation does not have a leading 1, so we need an exponent of zero to indicate a *denormalized* float which implies a leading zero in front of the significand. Fortunately, this nicely works out to represent zero as **0x00000000**.

#### e) 0xFF94BEEF

#### Answer: NaN

Certain exponent fields are reserved for representing special values. Floating point representations with exponents of 255 and a zero significand are reserved for  $\pm \infty$ , and exponents of 255 with a nonzero significand are reserved for representations of NaN. Deconstructing the fields of this number gives an exponent of **Ob11111111 = 255** and a nonzero significand which indicates that this represents NaN. Note that there are many possible ways to represent NaN.

### Answer: 0x7F800000

### g) 1/3

Answer: N/A - impossible to represent in single-precision floating point, we can only approximate it

# 2 More Floating Point

As we saw above, not every number can be represented perfectly using floating point. For this question, we will only look at positive numbers.

2.1 What is the next smallest number larger than 2 that can be represented completely?

Answer:  $2 + 2^{-22}$ 

First, we start at the number 2 and write it in the normalized form. Then we increment the number by the smallest amount possible, which is the same as incrementing the significand by 1 at the rightmost location, which adds  $2^{-22}$ .

Normalized: 2 = 10.000... = 1.000...00  $\times$  2<sup>1</sup>

Increment:  $2 = (1.000...00 + 2^{-23}) \times 2^1 = (1 + 2^{-23}) \times 2 = 2 + 2^{-22}$ 

2.2 What is the next smallest number larger than 4 that can be represented completely?

Answer:  $4 + 2^{-21}$ 

Similarly, we write 4 in its normalized form, and increment it by the smallest amount possible. This is the same as incrementing the significand by 1 at the rightmost location.

Normalized:  $4 = 100.000... = 1.000...00 \times 2^2$ 

Increment:  $(1.000...00 + 2^{-23}) \times 2^2 = (1 + 2^{-23}) \times 4 = 4 + 2^{-21}$ 

2.3 What is the largest odd number that we can represent? Hint: at what power can we only represent even numbers?

Answer:  $2^{24} - 1$ 

To find the largest odd number we can represent, we want to find when odd numbers will stop appearing. Because we are always multiplying the significand by a power of  $2^x$ , we will only be able to represent even numbers when the exponent grows large enough. In particular, odd numbers will stop appearing when the significand's LSB has a step size (distance between each successive number) of 2, so the largest odd number will be the first number with a step size of 2, subtracted by 1. After this number, only even numbers can be represented in floating point.

We can think of each binary digit in the significant as corresponding to a different power of 2 to get to a final sum. For example, 0b1011 can be evaluated as  $2^3 + 2^1 + 2^0$ , where the MSB is the 3rd bit and corresponds to  $2^3$  and the LSB is the 0th bit at  $2^0$ .

We want our LSB to correspond to  $2^1$ , so by counting the number of mantissa bits (23) and including the implicit 1, we get a total exponent of 24. The smallest number with this power would have a mantissa of 00..00, so after taking account of the implicit 1 and subtracting, this gives  $2^{24} - 1$ 

## 3 RISC-V Instructions

3.1 Assume we have an array in memory that contains int \*arr = {1,2,3,4,5,6,0}. Let register s0 hold the address of the element at index 0 in arr. You may assume integers are four bytes and our values are word-aligned. What do the following snippets of RISC-V code do? Assume that all the instructions are run one after the other in the same context.

a) lw t0, 12(s0)

Answer: Sets t0 equal to arr[3]

b) sw t0, 16(s0)

Answer: Stores t0 into arr [4]

c) slli t1, t0, 2 add t2, s0, t1 lw t3, 0(t2) addi t3, t3, 1 sw t3, 0(t2)

Answer: Increments **arr**[4] by 1.

1st line sets t1 = 16

2nd line adds it to **s0** so that it now points at **arr**[4]

3rd-5th line loads the value at arr [4], increments by one, and stores it back

```
d) lw t0, 0(s0)
    xori t0, t0, 0xFFF
    addi t0, t0, 1
```

Answer: Sets t0 to -1 \* arr[0]

# 4 RISC-V Memory Access

Using the given instructions and the sample memory array, what will happen when the RISC-V code is executed? For load instructions (1w, 1b, 1h), write out what each register will store. For store instructions (sw, sh, sb), update the memory array accordingly. Recall that RISC-V is little-endian and byte addressable. For any unknown instructions, use the <u>CS 61C reference card!</u>

### 4.1

li t0 0x00FF0000 lw t1 0(t0) addi t0 t0 4 lh t2 2(t0)	OxFFFFFFFF	
	0x00FF0004	0x000C561C
lw s0 0(t1)	0x00FF0000	36
lb s1 3(t2)		
	0x0000036	OxFDFDFDFD
	0x0000024	OxDEADB33F
	0x000000C	0xC5161C00
	0x00000000	
What value does each register hold after the code is executed?		

What value does each register hold after the code is executed?

t0: 0x00FF0004. Line 3 adds 4 to the initial address.

t1: 36. Line 2 loads the 4-byte word from address 0x00FF0000.

t2: 0xC. Line 4 loads two bytes starting at the address 0x00FF0004 + 2 = 0x00FF0006. This returns 0x000C

s0: 0xDEADB33F. Line 5 loads the word starting at address 36 = 0x24 which is 0xDEADB33F.

**s1**: **0xFFFFFC5**. Line 6 loads the MSB starting of the 4-byte word at address **0xC**. The value is **0xC5** which is sign-extended to **0xFFFFFC5**.

4.2 Update the memory array with its new values after the code is executed. Assume each byte in the memory array is initialized to zero.

li tO OxABADCAF8	OxFFFFFFFF	0x00000000
li t1 0xF9120504		
li t2 OxBEEFDABO	0xF9120504	OxABADCAF8
sw t0 0(t1)	0.110120001	oning ing on o
addi t0 t0 4		•••
sh t1 2(t0)	OxBEEFDABO	0x00000000
sh t2 0(t0)		
lw t3 O(t1)	OXABADCAFC	0x0504DAB0
sb t1 1(t3)		
sb t2 3(t3)	OxABADCAF8	0xB0000400
		•••
	0x00000000	0x00000000

# 5 Lost in Translation

5.1 Translate the code verbatim between C and RISC-V. The comments above the code indicate which registers to store the variables.

These code snippets are a great reference for writing RISC-V code!

С	RISC-V
<pre>// s0 -&gt; a // s1 -&gt; b // s2 -&gt; c // s3 -&gt; z int a = 4, b = 5, c = 6;</pre>	addi s0, x0, 4 addi s1, x0, 5 addi s2, x0, 6 add s3, s0, s1 add s3, s3, s2
int z = a + b + c + 10;	addi s3, s3, 10
<pre>// int *p = intArr; // s0 -&gt; p; // s1 -&gt; a; *p = 0; int a = 2; p[1] = p[a] = a;</pre>	<pre>sw x0, 0(s0) addi s1, x0, 2 sw s1, 4(s0) slli t0, s1, 2 add t0, t0, s0 sw s1, 0(t0)</pre>

С	RISC-V
<pre>// s0 -&gt; a, // s1 -&gt; b int a = 5; int b = 10; if (a + a == b) { a = 0; } else { b = a - 1; }</pre>	<pre>start: addi s0, x0, 5 addi s1, x0, 10 add t0, s0, s0 bne t0, s1, else add s0, x0, x0 jal x0, exit else: addi s1, s0, -1 exit: </pre>
<pre>// Compute s1 = 2^30 int s0 = 0; int s1 = 1; for (; s0 != 30; s0 += 1) {    s1 *= 2; }</pre>	<pre>start: addi s0, x0, 0 addi s1, x0, 1 addi t0, x0, 30 loop: beq s0, t0, exit slli s1, s1, 1 addi s0, s0, 1 jal x0, loop exit: </pre>
<pre>// s0 -&gt; n // s1 -&gt; sum for (int sum = 0; n &gt; 0; n) sum += n; }</pre>	<pre>start: addi s1, x0, 0 loop: beq s0, x0, exit add s1, s1, s0 addi s0, s0, -1 jal x0, loop exit: </pre>